

Seminar

Concurrency Theory

Initial Meeting

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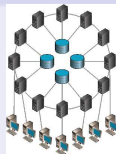
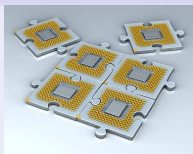
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Updated version! November 14, 2011
Deadlines have been shifted!

Why concurrency theory?

Example of concurrency

- Multi-core processors
- Distributed computing



Challenges

Parallelism induces **uncertainty**.

How to describe concurrent behavior?

- Interleaving semantics
- True concurrency



Learning objectives

Learn about concurrency

What theoretical approaches exist to reason about concurrency?

- Which formalism is best suited to model a specific aspect of a system?
- Different ways to think about concurrency.
- **Decidability** results.

Learn how to work scientifically

- Grasp the essence of a research topic and understand it thoroughly.
- Find references and additional papers in the scope of your topic.
- Write a scientific seminar paper on your topic.
- Give a talk and present scientific results comprehensively.

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Topics in concurrency theory

Interleaving concurrency

One step at a time, **completely ordered**.

versus

True concurrency (non-interleaving concurrency)

Order of events (transitions, steps, etc.) remains **partial**, **causality**.

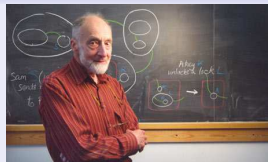
Process calculi: CCS

A complete axiomatisation of observational congruence

- Strong bisimulation is too fine grained.
- Weak bisimulation is too coarse.

⇒ **Observational congruence!**

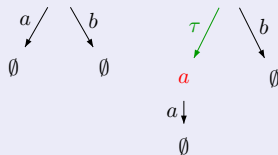
This topic is on a complete axiomatisation of observational congruence for finite CCS processes.



Weak bisimulation:

$$a \approx_{\text{weak}} \tau.a \text{ and } b \approx_{\text{weak}} b \dots$$

But: $a + b \not\approx_{\text{weak, obs}} \tau.a + b$



Observational congruence: $a \not\approx_{\text{obs}} \tau.a$

Barbed bisimulation

- **Reduction** vs. **interaction**.
- Another derivation of strong bisimulation.
- Inspired by reduction in term rewrite systems.
- τ -steps and reduction.

Comparing recursion, replication, and iteration in process calculi

Extend CCS to infinite behaviors:

Recursion, Replication, and Iteration.

$$P ::= \emptyset \mid \alpha.P \mid P_1 + P_2 \mid \\ P_1 \parallel P_2 \mid P \setminus L \mid \\ A(x_1, \dots, x_n) \mid !P \mid P^*$$

Questions that arise in this topic are:

- How to extend CCS with iteration?
- How are recursion, replication and iteration related?
- Can one encode the other?
- Decidability results for convergence and weak bisimilarity.

Decidable subsets of CCS

- Strong bisimilarity **undecidable** for full CCS.
- Which **subsets** of CCS make it decidable?

$$P ::= \emptyset \mid \alpha.P \mid P_1 + P_2 \mid \\ P_1 \parallel P_2 \mid P \setminus L \mid \\ A(x_1, x_2, \dots, x_n)$$

$$\Delta = \{X_i \equiv P_i \mid 1 \leq i \leq k\}$$

Process calculi: π -calculus

Foundations of the π -calculus

- CCS' communication structure is **static**.
- π -calculus for **mobile** processes.
- Two entities: **names** and **processes**.

Topics: **Theoretical foundations** of the π -calculus.

Classical notions of **bisimulation** in the π -calculus.

$$\begin{aligned} P ::= & \emptyset \mid \\ & x(y).P \mid \\ & \bar{x} \langle y \rangle P \mid \\ & [x == b] P \mid \\ & P_1 \parallel P_2 \mid \\ & (\nu x)P \mid \\ & !P \end{aligned}$$

Process calculi: π -calculus

A theory of bisimulation for the π -calculus

Classical bisimulations do not preserve all π -calculus operators.

- Ground bisimulation (not preserved under **parallel composition**)

$$P \xrightarrow{a} P' \implies Q \xrightarrow{a} Q' \text{ for some } Q' \text{ s.t. } P' \sim_g Q'$$

- Late bisimulation (not preserved under **prefixing**)

$$P \xrightarrow{a(x)} P' \implies Q \xrightarrow{a(x)} Q' \text{ for some } Q' \text{ s.t. for all } y. P' [y/x] \sim_l Q' [y/x]$$

Topic: **A better bisimulation** which

- preserves all π -calculus operators.
- Bisimulation for CCS + X .

$$\begin{array}{ccc} a(x). [x == b]. \bar{b}b & \begin{array}{c} \sim_g \\ \not\sim_l \end{array} & a(x). \emptyset \\ \downarrow a(x) & & \downarrow a(x) \\ [x == b]. \bar{b}b & \begin{array}{c} \sim_g \\ \sim_l \end{array} & \emptyset \end{array}$$

$$a(x). [x == b]. \bar{b}b \parallel \bar{a}b \not\sim_g a(x). \emptyset \parallel \bar{a}b$$

Process calculi: The spi-calculus

Introduction of the spi calculus

- Extension of the π -calculus to model **cryptographic protocols**.
- Extend π -calculus with notions of
 - encryption
 - decryption



The theory of the Psi-calculus

- General extension the π -calculus
- With nominal data
- Data terms, conditions and assertions

Mobile ambients

- Mobility: **Computing nodes** and **data!**
- Ambient: Where computation happens.
- Agents: Processes.
- Ambients have associated processes.
- Ambients can be nested and move.

Modal transition systems and interface theories

- **Modal transition systems**
- Modalities (necessary and admissible behavior)
- Refinement.
- Extend process algebra towards specification logic!
- **Interface theories**

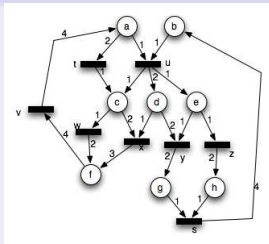
I/O automata

- Automata-based interface language
- Assumptions about environment
- Guarantees about component's behavior
- Extend interface automata to modal I/O automata.

Non-interleaving models of concurrency

Undecidability of bisimilarity for Petri nets

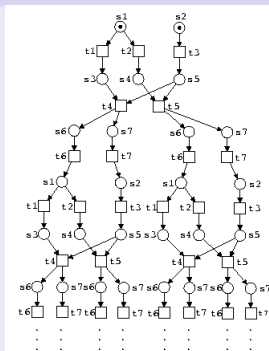
- Petri nets as a true-concurrency model
- **Undecidability of bisimilarity** in Petri nets
- Proof by reduction of the halting problem of **counter machines**.
- Further decidability results



Non-interleaving models of concurrency

Branching processes of Petri nets

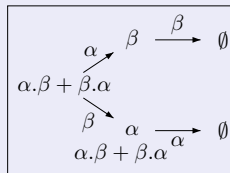
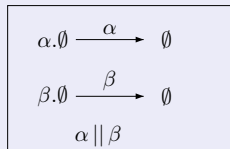
- Branching process = **initial run** of a Petri net
- **Partial order** on branching processes
- Unfolding of Petri nets
- Basis for **event structures**.



Non-interleaving models of concurrency

The relation between CCS and Petri nets

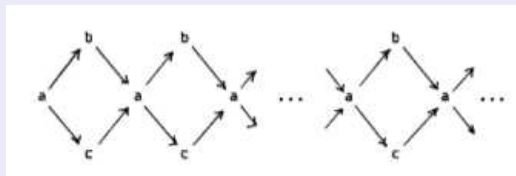
- Usually, CCS has a **interleaving semantics**.
- $\alpha \parallel \beta$ and $\alpha.\beta + \beta.\alpha$ coincide in classical CCS.
- But not here:
 - CCS semantics defined by Petri nets
 - No **linear** but a **causal** order on events



Non-interleaving models of concurrency

Trace theory and Mazurkiewicz traces

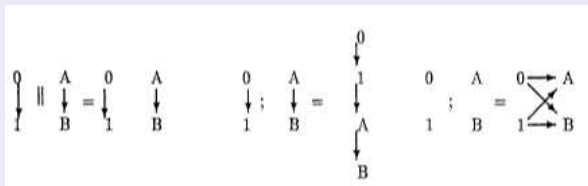
- Traces describe processes
- Not sequential, but partially ordered
- **Non-interleaving semantics**
- Strings vs. traces



Non-interleaving models of concurrency

Modeling concurrency with partial orders

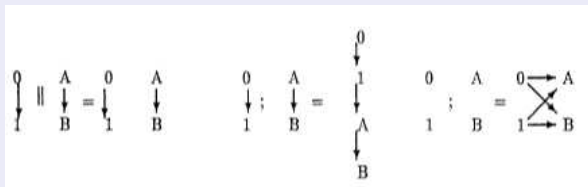
- Partial string: **partially ordered multiset (Pomset)**
- Set of partial strings: Processes



Non-interleaving models of concurrency

Comparing Pomsets and Mazurkiewicz traces

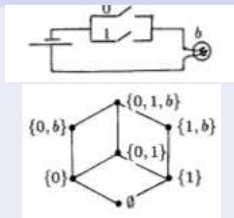
- Trade-off between Pomsets and Mazurkiewicz traces:
- Mazurkiewicz traces are restricted subclass of Pomsets
- **Pomsets more general**
- **Mazurkiewicz traces have more structure**



Non-interleaving models of concurrency

Event structures

- Processes execute **events**.
 - consistent (events may prevent others)
 - enabling: (sequence of events)
- **Configurations** are the state of a process,
- they are partially ordered: **progress**.



Expectations

Seminar paper

- Prepare a seminar paper of **max. 20 pages**.
- Include a complete list of **references** and **cite correctly**.
- **Plagiarism:**
Copying content from other sources without citation leads to disqualification.
- Font size 11pt with the usual page dimensions.
- Language is **English**.
- We expect **proper language** if you hand in your drafts:
 ≥ 10 typos per page \implies no further corrections

The final seminar papers are distributed **at least a week before** the talks.
 \implies Read other participants' papers!

Expectations

Seminar talk

- You give a scientific talk of **30 minutes**.
- Present your topic according to the audience.
Goal: Participants should be able to follow you!
- **Well structured** slides:
 - Not more than ~ 10 lines of text per slide.
 - Sensible use of colors
 - Select the important aspects and present them formally.
 - Use examples and figures to motivate theory.
- The talk will be given in **English**.

Be prepared to ask questions and to discuss about the seminar's topics.

Organisation

Schedule for the seminar paper (Attention: Schedule changed!)

- November 21: Last possibility to withdraw from the seminar.
- December 5: Hand in the structure of your paper.
Be prepared to discuss about your topic!
- January 11: Hand in the seminar paper.
- February 1: Final version of seminar paper due.
- February 15: Hand in preliminary version of slides.
- March 7: Final version of slides due.
- March 12 & 13: “Mini conference” with seminar talks.

Handling of deadlines

- All **deadlines** in this seminar are **strict**.
Missing a deadline disqualifies from further participation.
- Participation during the talks is **mandatory**.



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